

# Package: npDoseResponse (via r-universe)

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**Type** Package

**Title** Nonparametric Estimation and Inference on Dose-Response Curves

**Version** 0.1

**Description** A novel integral estimator for estimating the causal effects with continuous treatments (or dose-response curves) and a localized derivative estimator for estimating the derivative effects. The inference on the dose-response curve and its derivative is conducted via nonparametric bootstrap. The reference paper is Zhang, Chen, and Giessing (2024) <[doi:10.48550/arXiv.2405.09003](https://doi.org/10.48550/arXiv.2405.09003)>.

**URL** <https://github.com/zhangyk8/npDoseResponse/>

**BugReports** <https://github.com/zhangyk8/npDoseResponse/issues>

**License** MIT + file LICENSE

**Encoding** UTF-8

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**Suggests** locpol

**Maintainer** Yikun Zhang <[yikunzhang@foxmail.com](mailto:yikunzhang@foxmail.com)>

**NeedsCompilation** no

**Author** Yikun Zhang [aut, cre]  
(<<https://orcid.org/0000-0003-3905-6346>>), Yen-Chi Chen [aut]  
(<<https://orcid.org/0000-0002-4485-306X>>)

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|             |   |
|-------------|---|
| DerivEffect | <i>The proposed localized derivative estimator.</i> |
|-------------|---|

---

## Description

This function implements our proposed estimator for estimating the derivative of a dose-response curve via Nadaraya-Watson conditional CDF estimator.

## Usage

```
DerivEffect(
  Y,
  X,
  t_eval = NULL,
  h_bar = NULL,
  kernT_bar = "gaussian",
  h = NULL,
  b = NULL,
  C_h = 7,
  C_b = 3,
  print_bw = TRUE,
  degree = 2,
  deriv_ord = 1,
  kernT = "epanechnikov",
  kernS = "epanechnikov",
  parallel = TRUE,
  cores = 6
)
```

## Arguments

|   |   |
|---|---|
| Y | The input n-dimensional outcome variable vector.  |
| X | The input n*(d+1) matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables. |

|              |  |
|--------------|--|
| t_eval       | The m-dimensional vector for evaluating the derivative. (Default: t_eval = NULL. Then, t_eval = X[,1], which consists of the observed treatment variables.)  |
| h_bar        | The bandwidth parameter for the Nadaraya-Watson conditional CDF estimator. (Default: h_bar = NULL. Then, the Silverman's rule of thumb is applied. See Chen et al. (2016) for details.)  |
| kernT_bar    | The name of the kernel function for the Nadaraya-Watson conditional CDF estimator. (Default: "gaussian".)  |
| h, b         | The bandwidth parameters for the treatment/exposure variable and confounding variables in the local polynomial regression. (Default: h = NULL, b = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_h and C_b, respectively.) |
| C_h, C_b     | The scaling factors for the rule-of-thumb bandwidth parameters.  |
| print_bw     | The indicator of whether the current bandwidth parameters should be printed to the console. (Default: print_bw = TRUE.)  |
| degree       | Degree of local polynomials. (Default: degree = 2.)  |
| deriv_ord    | The order of the estimated derivative of the conditional mean outcome function. (Default: deriv_ord = 1. It shouldn't be changed in most cases.)   |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".)  |
| parallel     | The indicator of whether the function should be parallel executed. (Default: parallel = TRUE.)   |
| cores        | The number of cores for parallel execution. (Default: cores = 6.)  |

### Value

The estimated derivative of the dose-response curve evaluated at points t\_eval.

### Author(s)

Yikun Zhang, <yikunzhang@foxmail.com>

### References

- Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.
- Hall, P., Wolff, R. C., and Yao, Q. (1999) *Methods for Estimating A Conditional Distribution Function*. *Journal of the American Statistical Association*, 94 (445): 154-163.

### Examples

```
library(parallel)
set.seed(123)
n <- 300

S2 <- cbind(2 * runif(n) - 1, 2 * runif(n) - 1)
```

```

Z2 <- 4 * S2[, 1] + S2[, 2]
E2 <- 0.2 * runif(n) - 0.1
T2 <- cos(pi * Z2^3) + Z2 / 4 + E2
Y2 <- T2^2 + T2 + 10 * Z2 + rnorm(n, mean = 0, sd = 1)
X2 <- cbind(T2, S2)

t_qry2 = seq(min(T2) + 0.01, max(T2) - 0.01, length.out = 100)
chk <- Sys.getenv("_R_CHECK_LIMIT_CORES_", "")
if (nzchar(chk) && chk == "TRUE") {
  # use 2 cores in CRAN/Travis/AppVeyor
  num_workers <- 2L
} else {
  # use all cores in devtools::test()
  num_workers <- parallel::detectCores()
}
theta_est2 = DerivEffect(Y2, X2, t_eval = t_qry2, h_bar = NULL,
                        kernT_bar = "gaussian", h = NULL, b = NULL,
                        C_h = 7, C_b = 3, print_bw = FALSE,
                        degree = 2, deriv_ord = 1, kernT = "epanechnikov",
                        kernS = "epanechnikov", parallel = TRUE, cores = num_workers)
plot(t_qry2, theta_est2, type="l", col = "blue", xlab = "t", lwd=5,
     ylab="(Estimated) derivative effects")
lines(t_qry2, 2*t_qry2 + 1, col = "red", lwd=3)
legend(-2, 5, legend=c("Estimated derivative", "True derivative"),
      fill = c("blue","red"))

```

---

DerivEffectBoot

*Nonparametric bootstrap inference on the derivative effect via our localized derivative estimator.*


---

## Description

This function implements the nonparametric bootstrap inference on the derivative of a dose-response curve via our localized derivative estimator.

## Usage

```

DerivEffectBoot(
  Y,
  X,
  t_eval = NULL,
  boot_num = 500,
  alpha = 0.95,
  h_bar = NULL,
  kernT_bar = "gaussian",
  h = NULL,
  b = NULL,

```

```

    C_h = 7,
    C_b = 3,
    print_bw = TRUE,
    degree = 2,
    deriv_ord = 1,
    kernT = "epanechnikov",
    kernS = "epanechnikov",
    parallel = TRUE,
    cores = 6
)

```

### Arguments

|              |  |
|--------------|--|
| Y            | The input n-dimensional outcome variable vector.   |
| X            | The input n*(d+1) matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables.  |
| t_eval       | The m-dimensional vector for evaluating the derivative. (Default: t_eval = NULL. Then, t_eval = X[, 1], which consists of the observed treatment variables.)   |
| boot_num     | The number of bootstrapping times. (Default: boot_num = 500.)  |
| alpha        | The confidence level of both the uniform confidence band and pointwise confidence interval. (Default: alpha = 0.95.)   |
| h_bar        | The bandwidth parameter for the Nadaraya-Watson conditional CDF estimator. (Default: h_bar = NULL. Then, the Silverman's rule of thumb is applied. See Chen et al. (2016) for details.)  |
| kernT_bar    | The name of the kernel function for the Nadaraya-Watson conditional CDF estimator. (Default: kernT_bar = "gaussian".)  |
| h, b         | The bandwidth parameters for the treatment/exposure variable and confounding variables in the local polynomial regression. (Default: h = NULL, b = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_h and C_b, respectively.) |
| C_h, C_b     | The scaling factors for the rule-of-thumb bandwidth parameters.  |
| print_bw     | The indicator of whether the current bandwidth parameters should be printed to the console. (Default: print_bw = TRUE.)  |
| degree       | Degree of local polynomials. (Default: degree = 2.)  |
| deriv_ord    | The order of the estimated derivative of the conditional mean outcome function. (Default: deriv_ord = 1. It shouldn't be changed in most cases.)   |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".)  |
| parallel     | The indicator of whether the function should be parallel executed. (Default: parallel = TRUE.)   |
| cores        | The number of cores for parallel execution. (Default: cores = 6.)  |

**Value**

A list that contains four elements.

`theta_est`        The estimated derivative of the dose-response curve evaluated at points `t_eval`.  
`theta_est_boot`   The estimated derivative of the dose-response curve evaluated at points `t_eval` for all the bootstrap samples.  
`theta_alpha`      The width of the uniform confidence band.  
`theta_alpha_var`   The widths of the pointwise confidence bands at evaluation points `t_eval`.

**Author(s)**

Yikun Zhang, <yikunzhang@foxmail.com>

**References**

Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.

**Examples**

```
set.seed(123)
n <- 300

S2 <- cbind(2 * runif(n) - 1, 2 * runif(n) - 1)
Z2 <- 4 * S2[, 1] + S2[, 2]
E2 <- 0.2 * runif(n) - 0.1
T2 <- cos(pi * Z2^3) + Z2 / 4 + E2
Y2 <- T2^2 + T2 + 10 * Z2 + rnorm(n, mean = 0, sd = 1)
X2 <- cbind(T2, S2)

t_qry2 = seq(min(T2) + 0.01, max(T2) - 0.01, length.out = 100)
chk <- Sys.getenv("_R_CHECK_LIMIT_CORES_", "")
if (nzchar(chk) && chk == "TRUE") {
  # use 2 cores in CRAN/Travis/AppVeyor
  num_workers <- 2L
} else {
  # use all cores in devtools::test()
  num_workers <- parallel::detectCores()
}

# Increase bootstrap times "boot_num" to a larger integer in practice
theta_boot2 = DerivEffectBoot(Y2, X2, t_eval = t_qry2, boot_num = 3, alpha = 0.95,
                             h_bar = NULL, kernT_bar = "gaussian", h = NULL,
                             b = NULL, C_h = 7, C_b = 3, print_bw = FALSE,
                             degree = 2, deriv_ord = 1, kernT = "epanechnikov",
                             kernS = "epanechnikov", parallel = TRUE,
                             cores = num_workers)
```

IntegEst

*The proposed integral estimator.***Description**

This function implements our proposed integral estimator for estimating the dose-response curve.

**Usage**

```
IntegEst(
  Y,
  X,
  t_eval = NULL,
  h_bar = NULL,
  kernT_bar = "gaussian",
  h = NULL,
  b = NULL,
  C_h = 7,
  C_b = 3,
  print_bw = TRUE,
  degree = 2,
  deriv_ord = 1,
  kernT = "epanechnikov",
  kernS = "epanechnikov",
  parallel = TRUE,
  cores = 6
)
```

**Arguments**

|           |  |
|-----------|--|
| Y         | The input n-dimensional outcome variable vector.   |
| X         | The input n*(d+1) matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables.  |
| t_eval    | The m-dimensional vector for evaluating the dose-response curve. (Default: t_eval = NULL. Then, t_eval = X[, 1], which consists of the observed treatment variables.)  |
| h_bar     | The bandwidth parameter for the Nadaraya-Watson conditional CDF estimator. (Default: h_bar = NULL. Then, the Silverman's rule of thumb is applied. See Chen et al. (2016) for details.)  |
| kernT_bar | The name of the kernel function for the Nadaraya-Watson conditional CDF estimator. (Default: "gaussian".)  |
| h, b      | The bandwidth parameters for the treatment/exposure variable and confounding variables in the local polynomial regression. (Default: h = NULL, b = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_h and C_b, respectively.) |

|              |   |
|--------------|---|
| C_h, C_b     | The scaling factors for the rule-of-thumb bandwidth parameters.   |
| print_bw     | The indicator of whether the current bandwidth parameters should be printed to the console. (Default: print_bw = TRUE.)                                 |
| degree       | Degree of local polynomials. (Default: degree = 2.)   |
| deriv_ord    | The order of the estimated derivative of the conditional mean outcome function. (Default: deriv_ord = 1. It shouldn't be changed in most cases.)        |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".) |
| parallel     | The indicator of whether the function should be parallel executed. (Default: parallel = TRUE.)  |
| cores        | The number of cores for parallel execution. (Default: cores = 6.)   |

### Value

The estimated dose-response curve evaluated at points `t_eval`.

### Author(s)

Yikun Zhang, <yikunzhang@foxmail.com>

### References

Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.

### Examples

```
set.seed(123)
n <- 300

S2 <- cbind(2*runif(n) - 1, 2*runif(n) - 1)
Z2 <- 4 * S2[, 1] + S2[, 2]
E2 <- 0.2 * runif(n) - 0.1
T2 <- cos(pi * Z2^3) + Z2 / 4 + E2
Y2 <- T2^2 + T2 + 10 * Z2 + rnorm(n, mean = 0, sd = 1)
X2 <- cbind(T2, S2)

t_qry2 = seq(min(T2) + 0.01, max(T2) - 0.01, length.out = 100)
chk <- Sys.getenv("_R_CHECK_LIMIT_CORES_", "")
if (nzchar(chk) && chk == "TRUE") {
  # use 2 cores in CRAN/Travis/AppVeyor
  num_workers <- 2L
} else {
  # use all cores in devtools::test()
  num_workers <- parallel::detectCores()
}
m_est2 = IntegEst(Y2, X2, t_eval = t_qry2, h_bar = NULL, kernT_bar = "gaussian",
  h = NULL, b = NULL, C_h = 7, C_b = 3, print_bw = FALSE,
  degree = 2, deriv_ord = 1, kernT = "epanechnikov",
```



```

kernS = "epanechnikov", parallel = TRUE, cores = num_workers)

plot(t_qry2, m_est2, type="l", col = "blue", xlab = "t", lwd=5,
     ylab="(Estimated) dose-response curves")
lines(t_qry2, t_qry2^2 + t_qry2, col = "red", lwd=3)
legend(-2, 6, legend=c("Estimated curve", "True curve"), fill = c("blue","red"))

```

---

|              |   |
|--------------|---|
| IntegEstBoot | <i>Nonparametric bootstrap inference on the dose-response curve via our integral estimator.</i> |
|--------------|---|

---

### Description

This function implements the nonparametric bootstrap inference on the dose-response curve via our integral estimator.

### Usage

```

IntegEstBoot(
  Y,
  X,
  t_eval = NULL,
  boot_num = 500,
  alpha = 0.95,
  h_bar = NULL,
  kernT_bar = "gaussian",
  h = NULL,
  b = NULL,
  C_h = 7,
  C_b = 3,
  print_bw = TRUE,
  degree = 2,
  deriv_ord = 1,
  kernT = "epanechnikov",
  kernS = "epanechnikov",
  parallel = TRUE,
  cores = 4
)

```

### Arguments

|   |   |
|---|---|
| Y | The input n-dimensional outcome variable vector.  |
| X | The input n*(d+1) matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables. |

|              |  |
|--------------|--|
| t_eval       | The m-dimensional vector for evaluating the dose-response curve (Default: t_eval = NULL. Then, t_eval = X[, 1], which consists of the observed treatment variables.)   |
| boot_num     | The number of bootstrapping times. (Default: boot_num = 500.)  |
| alpha        | The confidence level of both the uniform confidence band and pointwise confidence interval. (Default: alpha = 0.95.)   |
| h_bar        | The bandwidth parameter for the Nadaraya-Watson conditional CDF estimator. (Default: h_bar = NULL. Then, the Silverman's rule of thumb is applied. See Chen et al. (2016) for details.)  |
| kernT_bar    | The name of the kernel function for the Nadaraya-Watson conditional CDF estimator. (Default: kernT_bar = "gaussian".)  |
| h, b         | The bandwidth parameters for the treatment/exposure variable and confounding variables in the local polynomial regression. (Default: h = NULL, b = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_h and C_b, respectively.) |
| C_h, C_b     | The scaling factors for the rule-of-thumb bandwidth parameters.  |
| print_bw     | The indicator of whether the current bandwidth parameters should be printed to the console. (Default: print_bw = TRUE.)  |
| degree       | Degree of local polynomials. (Default: degree = 2.)  |
| deriv_ord    | The order of the estimated derivative of the conditional mean outcome function. (Default: deriv_ord = 1. It shouldn't be changed in most cases.)   |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".)  |
| parallel     | The indicator of whether the function should be parallel executed. (Default: parallel = TRUE.)   |
| cores        | The number of cores for parallel execution. (Default: cores = 6.)  |

### Value

A list that contains four elements.

|             |   |
|-------------|---|
| m_est       | The estimated dose-response curve evaluated at points t_eval.                               |
| m_est_boot  | The estimated dose-response curve evaluated at points t_eval for all the bootstrap samples. |
| m_alpha     | The width of the uniform confidence band.   |
| m_alpha_var | The widths of the pointwise confidence bands at evaluation points t_eval.                   |

### Author(s)

Yikun Zhang, <yikunzhang@foxmail.com>

### References

Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.

**Examples**

```

set.seed(123)
n <- 300

S2 <- cbind(2 * runif(n) - 1, 2 * runif(n) - 1)
Z2 <- 4 * S2[, 1] + S2[, 2]
E2 <- 0.2 * runif(n) - 0.1
T2 <- cos(pi * Z2^3) + Z2 / 4 + E2
Y2 <- T2^2 + T2 + 10 * Z2 + rnorm(n, mean = 0, sd = 1)
X2 <- cbind(T2, S2)

t_qry2 = seq(min(T2) + 0.01, max(T2) - 0.01, length.out = 100)
chk <- Sys.getenv("_R_CHECK_LIMIT_CORES_", "")
if (nzchar(chk) && chk == "TRUE") {
  # use 2 cores in CRAN/Travis/AppVeyor
  num_workers <- 2L
} else {
  # use all cores in devtools::test()
  num_workers <- parallel::detectCores()
}

# Increase bootstrap times "boot_num" to a larger integer in practice
m_boot2 = IntegEstBoot(Y2, X2, t_eval = t_qry2, boot_num = 3, alpha=0.95,
                      h_bar = NULL, kernT_bar = "gaussian", h = NULL, b = NULL,
                      C_h = 7, C_b = 3, print_bw = FALSE, degree = 2,
                      deriv_ord = 1, kernT = "epanechnikov", kernS = "epanechnikov",
                      parallel = TRUE, cores = num_workers)

```

---

KernelRetrieval

*The helper function for retrieving a kernel function and its associated statistics.*


---

**Description**

This function helps retrieve the commonly used kernel function, its second moment, and its variance based on the name.

**Usage**

```
KernelRetrieval(name)
```

**Arguments**

name                    The lower-case full name of the kernel function.

**Value**

A list that contains three elements.

|           |   |
|-----------|---|
| KernFunc  | The interested kernel function.           |
| sigmaK_sq | The second moment of the kernel function. |
| K_sq      | The variance of the kernel function.      |

**Author(s)**

Yikun Zhang, <yikunzhang@foxmail.com>

**Examples**

```
kernel_result <- KernelRetrieval("epanechnikov")
kernT <- kernel_result$KernFunc
sigmaK_sq <- kernel_result$sigmaK_sq
K_sq <- kernel_result$K_sq
```

---

LocalPolyReg

*The (partial) local polynomial regression.*

---

**Description**

This function implements the (partial) local polynomial regression for estimating the conditional mean outcome function and its partial derivatives. We use higher-order local monomials for the treatment variable and first-order local monomials for the confounding variables.

**Usage**

```
LocalPolyReg(  
  Y,  
  X,  
  x_eval = NULL,  
  degree = 2,  
  deriv_ord = 1,  
  h = NULL,  
  b = NULL,  
  C_h = 7,  
  C_b = 3,  
  print_bw = TRUE,  
  kernT = "epanechnikov",  
  kernS = "epanechnikov"  
)
```

**Arguments**

|              |  |
|--------------|--|
| Y            | The input n-dimensional outcome variable vector.   |
| X            | The input $n \times (d+1)$ matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables.   |
| x_eval       | The $n \times (d+1)$ matrix for evaluating the local polynomial regression estimates. (Default: x_eval = NULL. Then, x_eval = X.)  |
| degree       | Degree of local polynomials. (Default: degree = 2.)  |
| deriv_ord    | The order of the estimated derivative of the conditional mean outcome function. (Default: deriv_ord = 1.)  |
| h            | The bandwidth parameter for the treatment/exposure variable. (Default: h = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_h.) |
| b            | The bandwidth vector for the confounding variables. (Default: b = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_b.)          |
| C_h          | The scaling factor for the rule-of-thumb bandwidth parameter h.  |
| C_b          | The scaling factor for the rule-of-thumb bandwidth vector b.   |
| print_bw     | The indicator of whether the current bandwidth parameters should be printed to the console. (Default: print_bw = TRUE.)  |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".)  |

**Value**

The estimated conditional mean outcome function or its partial derivatives evaluated at points x\_eval.

**Author(s)**

Yikun Zhang, <yikunzhang@foxmail.com>

**References**

- Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.
- Fan, J. and Gijbels, I. (1996) *Local Polynomial Modelling and its Applications*. Chapman & Hall/CRC.

**Examples**

```
library(parallel)
set.seed(123)
n <- 300
S2 <- cbind(2 * runif(n) - 1, 2 * runif(n) - 1)
Z2 <- 4 * S2[, 1] + S2[, 2]
E2 <- 0.2 * runif(n) - 0.1
```

```

T2 <- cos(pi * Z2^3) + Z2 / 4 + E2
Y2 <- T2^2 + T2 + 10 * Z2 + rnorm(n, mean = 0, sd = 1)
X2 <- cbind(T2, S2)
t_qry2 = seq(min(T2) + 0.01, max(T2) - 0.01, length.out = 100)
chk <- Sys.getenv("_R_CHECK_LIMIT_CORES_", "")
if (nzchar(chk) && chk == "TRUE") {
  # use 2 cores in CRAN/Travis/AppVeyor
  num_workers <- 2L
} else {
  # use all cores in devtools::test()
  num_workers <- parallel::detectCores()
}
Y_est2 = LocalPolyReg(Y2, X2, x_eval = NULL, degree = 2, deriv_ord = 0,
                      h = NULL, b = NULL, C_h = 7, C_b = 3, print_bw = TRUE,
                      kernT = "epanechnikov", kernS = "epanechnikov")

```

---

LocalPolyRegMain

*The main function of the (partial) local polynomial regression.*


---

### Description

This function implements the main part of the (partial) local polynomial regression for estimating the conditional mean outcome function and its partial derivatives.

### Usage

```

LocalPolyRegMain(
  Y,
  X,
  x_eval = NULL,
  degree = 2,
  deriv_ord = 1,
  h = NULL,
  b = NULL,
  kernT = "epanechnikov",
  kernS = "epanechnikov"
)

```

### Arguments

|        |   |
|--------|---|
| Y      | The input n-dimensional outcome variable vector.  |
| X      | The input n*(d+1) matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables. |
| x_eval | The n*(d+1) matrix for evaluating the local polynomial regression estimates. (Default: x_eval = NULL. Then, x_eval = X.)                      |
| degree | Degree of local polynomials. (Default: degree = 2.)   |

|              |  |
|--------------|--|
| deriv_ord    | The order of the estimated derivative of the conditional mean outcome function. (Default: deriv_ord = 1.)  |
| h, b         | The bandwidth parameters for the treatment/exposure variable and confounding variables (Default: h = NULL, b = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_h and C_b, respectively.) |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".)  |

**Value**

The estimated conditional mean outcome function or its partial derivatives evaluated at points `x_eval`.

**Author(s)**

Yikun Zhang, <yikunzhang@foxmail.com>

**References**

Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.

Fan, J. and Gijbels, I. (1996) *Local Polynomial Modelling and its Applications*. Chapman & Hall/CRC.

---

RegAdjust

*The regression adjustment estimator of the dose-response curve.*

---

**Description**

This function implements the standard regression adjustment or G-computation estimator of the dose-response curve or its derivative via (partial) local polynomial regression.

**Usage**

```
RegAdjust(
  Y,
  X,
  t_eval = NULL,
  h = NULL,
  b = NULL,
  C_h = 7,
  C_b = 3,
  print_bw = TRUE,
  degree = 2,
  deriv_ord = 0,
  kernT = "epanechnikov",
```

```

kernS = "epanechnikov",
parallel = TRUE,
cores = 6
)

```

### Arguments

|              |  |
|--------------|--|
| Y            | The input n-dimensional outcome variable vector.   |
| X            | The input n*(d+1) matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables.  |
| t_eval       | The m-dimensional vector for evaluating the dose-response curve. (Default: t_eval = NULL. Then, t_eval = X[, 1], which consists of the observed treatment variables.)  |
| h, b         | The bandwidth parameters for the treatment/exposure variable and confounding variables (Default: h = NULL, b = NULL. Then, the rule-of-thumb bandwidth selector in Eq. (A1) of Yang and Tschernig (1999) is used with additional scaling factors C_h and C_b, respectively.) |
| C_h, C_b     | The scaling factors for the rule-of-thumb bandwidth parameters.  |
| print_bw     | The indicator of whether the current bandwidth parameters should be printed to the console. (Default: print_bw = TRUE.)  |
| degree       | Degree of local polynomials. (Default: degree = 2.)  |
| deriv_ord    | The order of the estimated derivative of the conditional mean outcome function. (Default: deriv_ord = 1.)  |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".)  |
| parallel     | The indicator of whether the function should be parallel executed. (Default: parallel = TRUE.)   |
| cores        | The number of cores for parallel execution. (Default: cores = 6.)  |

### Value

The estimated dose-response curves or its derivatives evaluated at points t\_eval.

### Author(s)

Yikun Zhang, <yikunzhang@foxmail.com>

### References

- Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.
- Fan, J. and Gijbels, I. (1996) *Local Polynomial Modelling and its Applications*. Chapman & Hall/CRC.



**Examples**

```

library(parallel)
set.seed(123)
n <- 300

S2 <- cbind(2 * runif(n) - 1, 2 * runif(n) - 1)
Z2 <- 4 * S2[, 1] + S2[, 2]
E2 <- 0.2 * runif(n) - 0.1
T2 <- cos(pi * Z2^3) + Z2 / 4 + E2
Y2 <- T2^2 + T2 + 10 * Z2 + rnorm(n, mean = 0, sd = 1)
X2 <- cbind(T2, S2)

t_qry2 = seq(min(T2) + 0.01, max(T2) - 0.01, length.out = 100)
chk <- Sys.getenv("_R_CHECK_LIMIT_CORES_", "")
if (nzchar(chk) && chk == "TRUE") {
  # use 2 cores in CRAN/Travis/AppVeyor
  num_workers <- 2L
} else {
  # use all cores in devtools::test()
  num_workers <- parallel::detectCores()
}
Y_RA2 = RegAdjust(Y2, X2, t_eval = t_qry2, h = NULL, b = NULL, C_h = 7, C_b = 3,
  print_bw = FALSE, degree = 2, deriv_ord = 0,
  kernT = "epanechnikov", kernS = "epanechnikov",
  parallel = TRUE, cores = num_workers)

```

---

RoTBWLocalPoly

*The rule-of-thumb bandwidth selector for the (partial) local polynomial regression.*


---

**Description**

This function implements the rule-of-thumb bandwidth selector for the (partial) local polynomial regression.

**Usage**

```

RoTBWLocalPoly(
  Y,
  X,
  kernT = "epanechnikov",
  kernS = "epanechnikov",
  C_h = 7,
  C_b = 3
)

```

**Arguments**

|              |   |
|--------------|---|
| Y            | The input n-dimensional outcome variable vector.  |
| X            | The input $n \times (d+1)$ matrix. The first column of X stores the treatment/exposure variables, while the other d columns are confounding variables.  |
| kernT, kernS | The names of kernel functions for the treatment/exposure variable and confounding variables. (Default: kernT = "epanechnikov", kernS = "epanechnikov".) |
| C_h, C_b     | The scaling factors for the rule-of-thumb bandwidth parameters.   |

**Value**

|   |  |
|---|--|
|   | A list that contains two elements.   |
| h | The rule-of-thumb bandwidth parameter for the treatment/exposure variable. |
| b | The rule-of-thumb bandwidth vector for the confounding variables.          |

**Author(s)**

Yikun Zhang, <yikunzhang@foxmail.com>

**References**

- Zhang, Y., Chen, Y.-C., and Giessing, A. (2024) *Nonparametric Inference on Dose-Response Curves Without the Positivity Condition*. <https://arxiv.org/abs/2405.09003>.
- Yang, L. and Tschernig, R. (1999). *Multivariate Bandwidth Selection for Local Linear Regression*. *Journal of the Royal Statistical Society Series B: Statistical Methodology*, 61(4), 793-815.

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